

Machine Learning-based Flexible Link Robot Control

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Abstract

Fuzzy systems have recently attracted the attention of researchers and various methods based on fuzzy logic systems have been presented. This paper presents a novel adaptive neuro fuzzy inference system based on interval Gaussian type-2 fuzzy sets in the antecedent part and Gaussian type-1 fuzzy sets as coefficients of linear combination of input variables in the consequent part. The capability of the proposed ANFIS2 for function approximation and dynamical system identification is remarkable. The structure of ANFIS2 is very similar to ANFIS but in ANFIS2 a layer is added for purpose to type reduction. An adaptive learning rate-based backpropagation with convergence guaranteed is used for parameter learning. Finally, the proposed ANFIS2 are used to control of a flexible link robot arm. Simulation results shows the proposed ANFIS2 with Gaussian type-1 fuzzy set as coefficients of linear combination of input variables in the consequent part has good performance and high accuracy but more training time.

Keywords

ANFIS, Interval Type-2 Fuzzy Sets, Inverse Control, Flexible Link Robot.

1. Introduction

High computation ability, adaptability and parallel processing are the important advantages of neural networks [1-5]. Using the knowledge of expert man as if-then rules and having real concept of parameters are the advantages of fuzzy systems. Among hybrid fuzzy neural networks, ANFIS is very popular and widespread. ANFIS is very simple and intelligible so it has affected many areas such as geography, medical Sciences, meteorological science, chemical and petroleum engineering and etc. [6-8]. A flexible link arm is a distributed parameter system of infinite order, but must be approximated by a lower-order model and controlled by a finite-order controller due to onboard computer limitations, sensor inaccuracy, and system noise. The so-called “control spillover” and “observation spillover” effects then occur, which under certain conditions can lead to instability [9,10].

In recent ten years, type-2 fuzzy logic with more capabilities and more flexibility than type-1 fuzzy logic has been investigated. Castillo et al. investigated type-2 fuzzy logic in more details [11]. Huang and Chen [12] used the combination of quantum inspired bacterial foraging algorithm (QBFA) and recursive least squares (RLS) to tune a type-2 fuzzy system. Tavooosi et al. proposed a different architecture of interval type-2 takagi-sugeno-kang fuzzy neural network [13-15]. They proposed an ANFIS based on type-2 fuzzy sets. Shahnazi [16] used type-2 fuzzy systems to approximate the unknown nonlinearities in MIMO systems control problem. He derived all the adaptive laws via Lyapunov synthesis approach.

Not much study has been done on fuzzy systems with type-1 (or type-2) fuzzy sets in the consequent part. In most of papers the consequent part is singleton [17] or interval type-1 fuzzy sets [18-20] up to now. In continue some of the works in this area are reviewed. In [21] interval type-2 fuzzy integrators in ensembles of ANFIS models for the time series prediction is used. Genetic algorithm is used to optimize of the proposed model. The equations of Type-2 ANFIS and its optimization are not presented. In [22] interval type-2 adaptive network-based fuzzy inference system with type-2 non-singleton fuzzification have introduced. Interval type-1 fuzzy sets have been used as consequent parameters. Mendez and Hernandez [23] presented a type-2 fuzzy ANFIS that interval type-1 non-singleton fuzzy numbers are the inputs and type-2 TSK FLS is the output and the consequent parameters are estimated by the recursive least-squares (RLS) method. They didn't provide further details of learning equations. Bhattacharyya et al. [24] proposed a type-2 fuzzy ANFIS that an interval type-2 fuzzy logic is used to combine the different outputs of the ANFIS classifiers to produce a final optimal result.

Tavooosi and Badamchizadeh proposed a type-2 Takagi-Sugeno-Kang fuzzy neural network with linear consequent part to system identification and modeling in [25]. Rule pruning was the novelty of that paper. Higher learning speed was the goal by reducing the parameter in both antecedent and consequent parts. Tavooosi et al. presented a new method to stability analysis of a class of type-2 fuzzy system in [26]. In [27], Jahangiri et al. proposed a method for stability analysis of a class of neural networks. In [28] a new method to MIMO type-2

fuzzy stability analysis has been presented. Robot manipulators have become increasingly important in the field of flexible automation. So, modeling and control of robots in automation will be very important. Some literatures used fuzzy logic to robot control [29-32].

This paper presents a novel ANFIS based on type-2 fuzzy named ANFIS2. The proposed method uses Interval Gaussian type-2 fuzzy sets in the antecedent part and Gaussian type-1 fuzzy sets as coefficients of linear combination of input variables in the consequent part. The paper is organized as follows. In section 2, type-2 fuzzy systems is viewed. In section 3, the structure of ANFIS2 is investigated. Parameter identification is given at the end of this section. In section 4, learning convergence of ANFIS2 based on lyapunov theory is derived. In section 5, the simulation studies are presented for identification of three nonlinear systems. Finally, Section 6 gives the conclusions of the advocated design methodology.

2. A Review on Type-2 Fuzzy Systems

In dealing with a lot of uncertainties, the performance and efficiency of type-1 fuzzy systems is not suitable. The membership degree of type-1 fuzzy sets is a crisp number while the membership degree of type-2 fuzzy sets is a type-1 fuzzy number.

Some difficulties of type-1 fuzzy logic can be solved by using type-2 fuzzy logic. In some systems such as time-series prediction, the exact membership degree is determined in a very difficult manner due to their complexity and their noisy information [33]. So, using type-2 fuzzy systems for describing behavior of these systems can be useful. In [34], some disadvantages of type-1 fuzzy sets are mentioned.

Fig. 1 shows the Gaussian primary membership function and Gaussian secondary membership function. For example, if $m = 0$, $\sigma = 1$ and $x = 1$ then degree of membership is 0.6, if this membership degree is too fuzzy or $\tilde{0.6}$ then primary membership is Gaussian type-1 fuzzy set with $m = 0$, $\sigma = 1$ and secondary membership is Gaussian type-1 fuzzy set with $m = 0.6$, $\sigma = 0.1$.

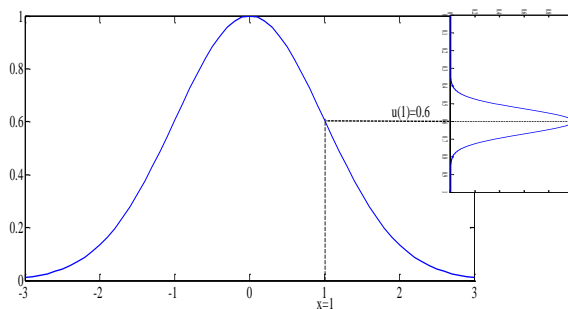


Fig. 1. Gaussian primary and secondary membership functions.

Note that, when secondary membership is not Gaussian type-1 fuzzy set and it is equal to one and in other words secondary membership function is interval set with one magnitude, then fuzzy set called interval type-2 fuzzy set.

Two cases of interval type-2 fuzzy sets are shown in Fig. 2. In Fig. 2-a, a case of a fuzzy set characterized by

a Gaussian membership function with mean m and a standard deviation that can take values in $[\sigma_1, \sigma_2]$ and in Fig. 2-b, a case of a fuzzy set with a Gaussian membership function with a fixed standard deviation σ , but an uncertain mean, taking values in $[m_1, m_2]$ and are shown.

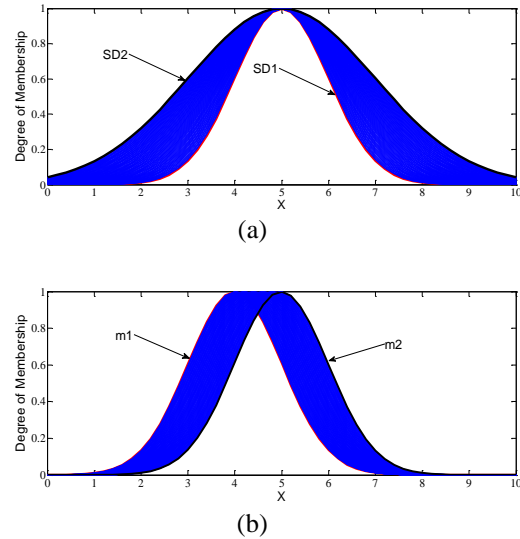


Fig. 2. a) Uncertainty in standard deviation b) uncertainty in mean.

In this paper Gaussian membership function with fixed standard deviation σ and uncertain mean is used (Fig. 2. b).

3. Adaptive Neuro Fuzzy Inference System by Type-2 Fuzzy Sets (ANFIS2)

Similar to type-1 TSK fuzzy systems, the output of type-2 TSK fuzzy systems is a function of their inputs. But in type-2 fuzzy systems the output and its coefficients are type-1 fuzzy sets. In this paper, the proposed ANFIS2 has seven layers that its structure is shown in Fig 3. The two rules of ANFIS2 can be described as follows:

$$R^1: \text{if } x_1 \text{ is } \tilde{A}_1 \text{ and } x_2 \text{ is } \tilde{B}_1 \text{ then } \tilde{y}_1 = \tilde{r}_1 + \tilde{p}_1 x_1 + \tilde{q}_1 x_2$$

$$R^2: \text{if } x_1 \text{ is } \tilde{A}_2 \text{ and } x_2 \text{ is } \tilde{B}_2^k \text{ then } \tilde{y}_2 = \tilde{r}_2 + \tilde{p}_2 x_1 + \tilde{q}_2 x_2 \quad (1)$$

Where $x_i (i = 1, 2)$ are inputs, $\tilde{y}_k (k = 1, 2)$ is output of the k th rule which it is type-1 fuzzy set (since it is a linear combination of Gaussian type-1 fuzzy sets), \tilde{A}_i^k are antecedent interval type-2 fuzzy sets, \tilde{r}_k , \tilde{p}_k and $\tilde{q}_k (k = 1, 2)$ are Gaussian type-1 fuzzy sets. For simplicity in description, we select only two inputs and two rules but the proposed ANFIS2 can be generalized to n -inputs and m -rules ($n, m \in N$).

The forward-propagation procedure is described as follows:

Layer 0: This layer is inputs layer. The number of nodes in this layer is equal to the number of inputs.

Layer 1: This layer is fuzzification layer. The output of this layer as follows:

$${}^1\mu_{k,i}(x_i, [\sigma_{k,i}, {}^1m_{k,i}]) = e^{-.5 \left(\frac{x_i - {}^1m_{k,i}}{\sigma_{k,i}} \right)^2} \quad (4)$$

$${}^2\mu_{k,i}(x_i, [\sigma_{k,i}, {}^2m_{k,i}]) = e^{-5\left(\frac{x_i - {}^2m_{k,i}}{\sigma_{k,i}}\right)^2} \quad (3)$$

Where $m_{k,i} \in [{}^1m_{k,i}, {}^2m_{k,i}]$ is uncertain mean for k th rule and i th input.

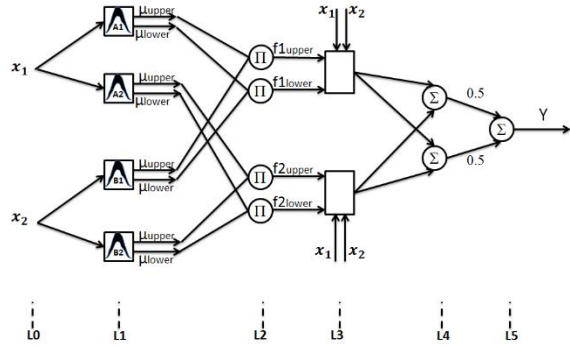


Fig. 3. The structure of ANFIS2.

$$\bar{\mu}_{k,i}(x_i) = \begin{cases} {}^1\mu_{k,i}(x_i, [\sigma_{k,i}, {}^1m_{k,i}]), & x_i < {}^1m_{k,i} \\ 1, & {}^1m_{k,i} \leq x_i \leq {}^2m_{k,i} \\ {}^2\mu_{k,i}(x_i, [\sigma_{k,i}, {}^2m_{k,i}]), & x_i > {}^2m_{k,i} \end{cases} \quad (4)$$

$$\underline{\mu}_{k,i}(x_i) = \begin{cases} {}^2\mu_{k,i}(x_i, [\sigma_{k,i}, {}^2m_{k,i}]), & x_i \leq \frac{{}^1m_{k,i} + {}^2m_{k,i}}{2} \\ {}^1\mu_{k,i}(x_i, [\sigma_{k,i}, {}^1m_{k,i}]), & x_i > \frac{{}^1m_{k,i} + {}^2m_{k,i}}{2} \end{cases} \quad (5)$$

Where $\bar{\mu}_{k,i}$ is upper membership degree and $\underline{\mu}_{k,i}$ is lower membership degree.

Layer 2: This is ruling layer. Each output node represents the lower (\underline{f}^k) and upper (\bar{f}^k) firing strength of a rule:

$$\underline{f}^k = \prod_{i=1}^n \underline{\mu}_{k,i} \quad ; \quad \bar{f}^k = \prod_{i=1}^n \bar{\mu}_{k,i} \quad (6)$$

Layer 3: This is consequent layer.

$$\begin{aligned} \tilde{y}_1 &= \tilde{r}_1 + \tilde{p}_1 x_1 + \tilde{q}_1 x_2 \\ \tilde{y}_2 &= \tilde{r}_2 + \tilde{p}_2 x_1 + \tilde{q}_2 x_2 \\ &\vdots \\ \tilde{y}_k &= \tilde{r}_k + \tilde{p}_k x_1 + \tilde{q}_k x_2 \end{aligned} \quad (7)$$

\tilde{r}_k, \tilde{p}_k and \tilde{q}_k ($k = 1, 2$) are consequent coefficient that they are Gaussian type-1 fuzzy sets. Note that (7) can be extended to \tilde{y}_k ($k = 1, \dots, n$). In this paper for simplicity $k = 2$.

Layer 4: This layer is used for consequent lower-upper firing points [35].

$$\hat{y}_l = \frac{\sum_{k=1}^N \bar{f}^k (m_{r_k} \sigma_{r_k} + m_{p_k} \sigma_{p_k} x_1 + m_{q_k} \sigma_{q_k} x_2) + \sum_{k=N+1}^M \underline{f}^k (m_{r_k} \sigma_{r_k} + m_{p_k} \sigma_{p_k} x_1 + m_{q_k} \sigma_{q_k} x_2)}{\sum_{k=1}^N \bar{f}^k (\sigma_{r_k} + \sigma_{p_k} + \sigma_{q_k}) + \sum_{k=N+1}^M \underline{f}^k (\sigma_{r_k} + \sigma_{p_k} + \sigma_{q_k})}$$

$$\hat{y}_r = \frac{\sum_{k=1}^L \underline{f}^k (m_{r_k} \sigma_{r_k} + m_{p_k} \sigma_{p_k} x_1 + m_{q_k} \sigma_{q_k} x_2) + \sum_{k=L+1}^P \bar{f}^k (m_{r_k} \sigma_{r_k} + m_{p_k} \sigma_{p_k} x_1 + m_{q_k} \sigma_{q_k} x_2)}{\sum_{k=1}^L \underline{f}^k (\sigma_{r_k} + \sigma_{p_k} + \sigma_{q_k}) + \sum_{k=L+1}^P \bar{f}^k (\sigma_{r_k} + \sigma_{p_k} + \sigma_{q_k})} \quad (8)$$

Layer 5: The single node in this layer computes the output.

$$\hat{y} = \frac{\hat{y}_l + \hat{y}_r}{2} \quad (9)$$

Gradient descent with adaptive learning rate backpropagation is used for learning phase [7].

4. Flexible Link Robot Arm

Consider a single-link robotic manipulator coupled to a brushed direct current motor with a no rigid joint. When the joint is modeled as a linear torsional spring, from the Euler-Lagrange equation, the equations of motion for such an electromechanical system can be derived as:

$$\begin{aligned} J_1 \ddot{q}_1 + F_1 \dot{q}_1 + K \left(q_1 - \frac{q_2}{N} \right) + mgd \cos q_1 &= 0 \\ J_2 \ddot{q}_2 + F_2 \dot{q}_2 + \frac{K}{N} \left(q_1 - \frac{q_2}{N} \right) &= K_t i \\ LDi + Ri + K_b \dot{q}_2 &= u \end{aligned} \quad (10)$$

where q_1 and q_2 are the angular positions of the link and the motor shaft, i is the armature current, and u is the armature voltage. The inertias J_1, J_2 , the viscous friction constants F_1, F_2 , the spring constant K , the torque constant K_t , the back-emf constant K_b , the armature resistance R and inductance L , the link mass M , the position of the link's center of gravity d , the gear ratio N and the acceleration of gravity g can all be unknown. A flexible link robot arm is shown in Fig. 4.

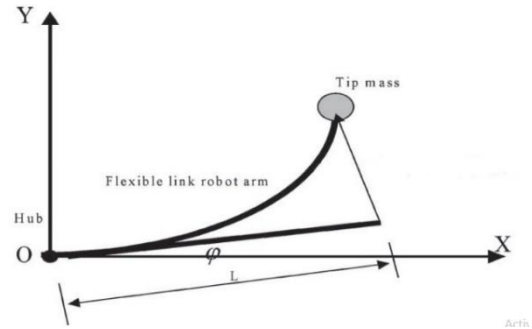


Fig. 4. Configuration of flexible-link robot arm.

5. Simulation Results

In this section, a flexible link robot arm is controlled using ANFIS2. The structure of the robot arm and ANFIS2 based controller is shown in Fig 5. Where the reference signal (desired angle in here) is applied to system then the error between reference signal and the output of robot system (angle of link in here) is calculated. This error must be minimized, so ANFIS2 is adapted to minimize the error.

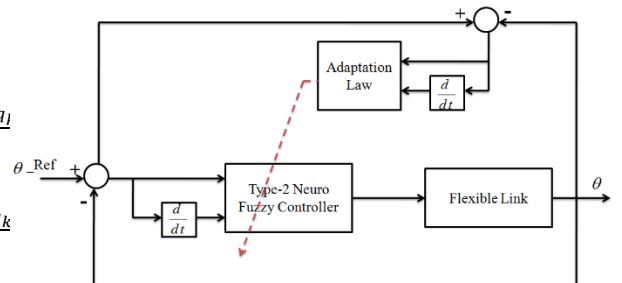


Fig. 5. The structure of the robot arm and ANFIS2 based controller.

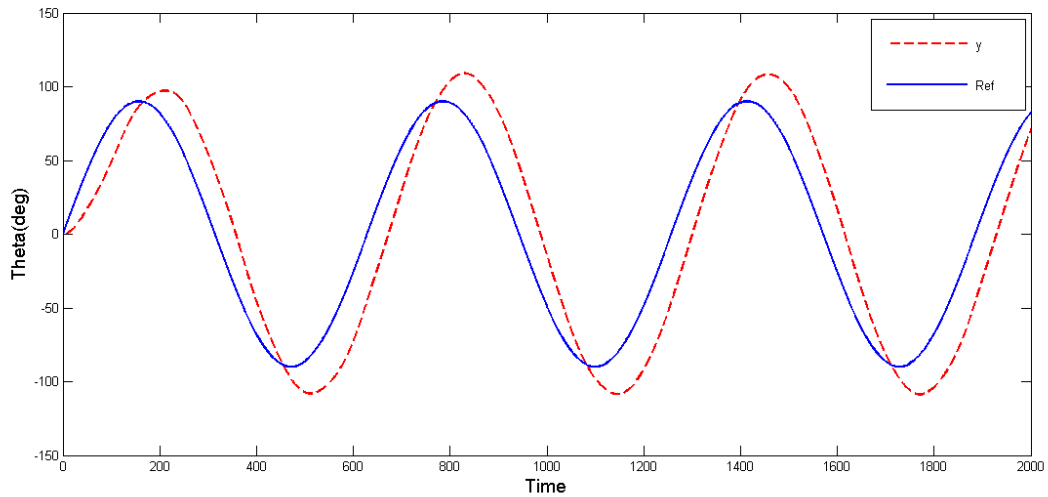


Fig. 6. ANFIS2 based controller with sine angle reference.

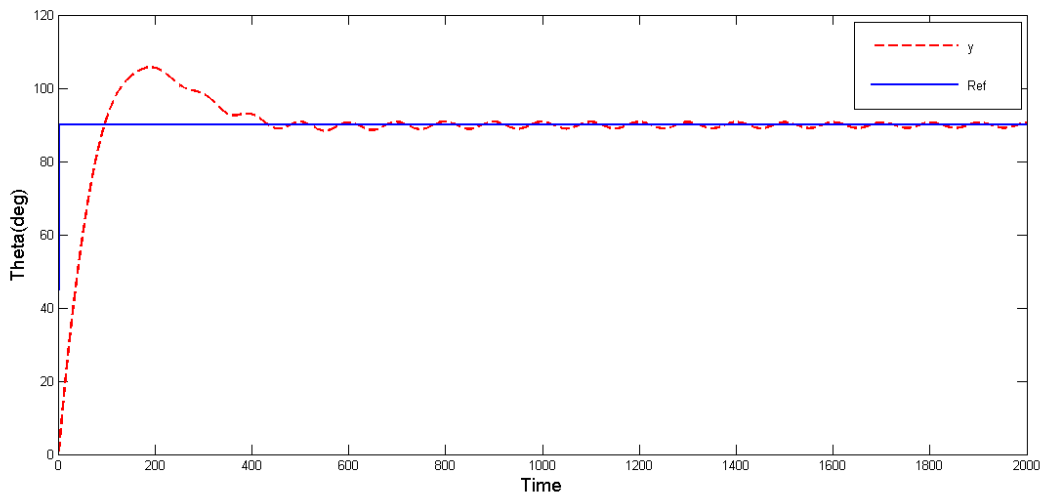


Fig. 7. ANFIS2 based controller with step angle reference.

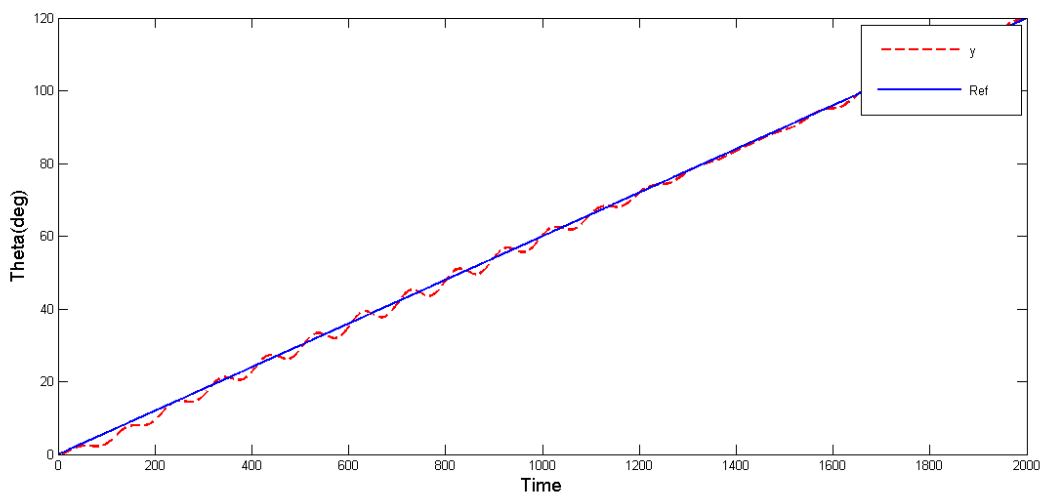


Fig. 8. ANFIS2 based controller with ramp angle reference.

In order to illustrate the effectiveness of the proposed results, the simulation will be conducted to control system, where $J_1 = 1.625 \text{ kg m}^2$, $J_2 = 1.625 \text{ kgm}^2$, $R = 0.5$ • , $K_t = 0.9 \text{ N m/A}$, $K = 0.5868$, $K_b = 0.9 \text{ N m/A}$, $M =$

4.34 kg , $L = 25.0 \times 10^{-3} \text{ H}$, $g = 9.8 \text{ N/kg}$, $F_1 = 1.625 \times 10^{-2} \text{ N m s/rad}$, $F_2 = 1.625 \times 10^{-2} \text{ N m s/rad}$, $N = 2$, $d = 0.5 \text{ m}$.

The performance of ANFIS2 with sine angle reference is shown in fig. 6 and the performance of ANFIS2 with step angle reference is shown in fig. 7. Also, figures 5-8 show that adaptive inverse control based on ANFIS2 is suitable and robust strategy to control of a flexible link robot arm.

6. Conclusion

In this paper, a novel ANFIS2 was proposed for identification of nonlinear dynamical systems. The proposed ANFIS2 is based on interval Gaussian type-2 fuzzy sets in the antecedent part and Gaussian type-1 fuzzy sets as coefficients of linear combination of input variables in the consequent part that it helps to improve modeling of highly nonlinear systems. Adaptive learning rate helps to prevent the ANFIS2 from trapping into a local minimum and it helps to fast convergence of training algorithm. The test results show the importance and necessity of ANFIS2 to modeling the inverse of uncertain systems and control it.

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